- 1 Conflicts are represented in a cognitive space to reconcile domain-general and
- 2 domain-specific cognitive control
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22 Abstract

- 23 Cognitive control resolves conflict between task-relevant and -irrelevant information 24 to enable goal-directed behavior. As conflict can arise from different sources (e.g., 25 sensory input, internal representations), how a finite set of cognitive control processes 26 can effectively address huge array of conflict remains a major challenge. We 27 hypothesize that different conflict can be parameterized and represented as distinct 28 points in a (low-dimensional) cognitive space, which can then be resolved by a 29 limited set of cognitive control processes working along the dimensions. To test this 30 hypothesis, we designed a task with five types of conflict that could be conceptually 31 parameterized along one dimension. Over two experiments, both human performance 32 and fMRI activity patterns in the right dorsolateral prefrontal (dlPFC) support that 33 different types of conflict are organized in a cognitive space. The findings suggest that 34 cognitive space can be a dimension reduction tool to effectively organize neural 35 representations of conflict for cognitive control. 36 37 Keywords: cognitive control, cognitive space, domain-general, domain-specific, 38 conflict
- 39

40 Introduction

41 Cognitive control enables humans to behave purposefully by modulating neural

42 processing to resolve conflict between task-relevant and task-irrelevant information.

43 For example, when naming the color of the word "BLUE" printed in red ink, we are

44 likely to be distracted by the word meaning, because reading a word is highly

45 automatic in daily life. To keep our attention on the color, we need to mobilize the

46 cognitive control processes to resolve the conflict between the color and word by
47 boosting/suppressing the processing of color/word meaning. As task-relevant and

- 48 task-irrelevant information can come from different sources, the sources of conflict
- 49 and how they should be resolved can vary greatly¹. For example, conflict may occur

50 between items of sensory information, such as between a red light and a police officer

51 signaling cars to pass. Alternatively, conflict may occur between sensory and motor

52 information, such as when a voice on the left asks you to turn right. The large variety

53 of conflict sources implies that there may be unlimited number of conflicts. A key

unsolved question in cognitive control is how our brain efficiently resolves a nearly
 infinite number of different types of conflict.

A first step to addressing this question is to examine the commonalities and/or dissociations across different types of conflict that can be categorized into different *domains*. Examples of the domains of conflict include experimental paradigm^{2,3}, sensory modality^{4,5}, or conflict type regarding the dimensional overlap of conflict processes^{6,7}.

Two solutions to resolving a wide range of conflict types are proposed. They
differ based on whether the same cognitive control mechanisms are applied across
domains. On the one hand, the *domain-general* cognitive control theories posit that

the frontoparietal cortex adaptively encodes task information and can thus flexibly 64 implement control strategies for different types of conflict. This is supported by the 65 generalizable control adjustment (i.e., encountering a conflict trial from one type can 66 facilitate conflict resolution of another type)^{2,8} and similar neural patterns^{9,10} across 67 distinct conflict tasks. A broader domain-general view holds that the frontoparietal 68 69 brain regions/networks are widely involved in multiple control demands well beyond 70 the conflict domain^{11,12}, which explains the remarkable flexibility in human behaviors. However, since domain-general processes are by definition likely shared by different 71 72 tasks, when we need to handle multiple task demands at the same time, the efficiency 73 of both tasks would be impaired due to resource competition or interference¹³. 74 Therefore, the domain-general processes is evolutionarily less advantageous for humans to deal with the diverse situations requiring high efficiency 14 . On the other 75 hand, the *domain-specific* theories argue that different types of conflict are handled by 76 77 distinct cognitive control processes (e.g., where and how information processing should be modulated)^{15,16}. However, according to the domain-specific view, the 78 potentially unlimited conflict situations require a large variety of preexisting control 79 80 processes, which is biologically implausible¹⁷.

81 To reconcile the two theories, researchers recently proposed that cognitive control 82 might be a mixture of domain-general and domain-specific processes. For instance, Freitas et al.¹⁸ found that trial-by-trial adjustment of control can generalize across two 83 conflict domains to different degrees, leading to domain-general (strong 84 85 generalization) or domain-specific (weak or no generalization) conclusions depending on the task settings of the consecutive conflict. Similarly, different brain networks 86 87 may show domain-generality (i.e., representing multiple conflicts) or domainspecificity (i.e., representing individual conflicts separately)^{7,19}. Even within the same 88 brain area (e.g., medial frontal cortex), Fu et al.²⁰ found that the neural population 89 90 activity can be factorized into orthogonal dimensions encoding both domain-general 91 and domain-specific conflict information, which can be selectively read out by downstream brain regions. While the mixture view provides an explanation for the 92 93 contradictory findings²¹, it suffers the same criticism as domain-specific cognitive 94 control theories, as it still requires unlimited cognitive control processes to fully cover 95 all possible conflicts.

A key to reconciling domain-general and domain-specific cognitive control is to 96 97 organize the nearly infinite possible types of conflict using a system with limited, dissociable dimensions. A construct with a similar function is the *cognitive space*²², 98 which extends the idea of cognitive map^{23} to the representation of abstract 99 100 information. Critically, the cognitive space view holds that the representations of 101 different abstract information are organized continuously and the locations of 102 representations in the cognitive space are determined by the similarity among the represented information²². 103

In the human brain, it has been shown that abstract^{23,24} and social²⁵ information can be represented in a cognitive space. For example, social hierarchies with two independent scores (e.g., popularity and competence) can be represented in a 2D cognitive space (one dimension for each score), such that each social item can be

located by its score in the two dimensions²⁵. In the field of cognitive control, recent 108 studies have begun to conceptualize different control states within a cognitive space²⁶. 109 For example, Fu et al.²⁰ mapped different conflict conditions to locations in a 110 low/high dimensional cognitive space to demonstrate the domain-general/domain-111 specific problems; Grahek et al.²⁷ used a cognitive space model of cognitive control 112 113 settings to explain behavioral changes in the speed-accuracy tradeoff. However, the 114 cognitive spaces proposed in these studies were only applicable to a limited number of control states involved in their designs. Therefore, it remains unclear whether there 115 is a cognitive space that can explain an unlimited number of control states, similar to 116 that of the spatial location²² and non-spatial knowledge²³. A challenge to answering 117 this question lies in how to construct control states with continuous levels of 118 similarity. Our recent work²⁸ showed that it is possible to manipulate continuous 119 conflict similarity by using a mixture of two independent conflict types with varying 120 ratios, which can be used to further examine the behavioral and neural evidence for 121 122 the cognitive space view. It is also unclear how the cognitive space of cognitive 123 control is encoded in the brain, although that of spatial locations and non-spatial abstract knowledge has been relatively well investigated in the medial temporal lobe, 124 medial prefrontal and orbitofrontal system^{22,23}. Recent research has suggested that the 125 abstract task structure could be encoded and implemented by the frontoparietal 126 127 network^{29,30}, but whether a similar neural system encodes the cognitive space of cognitive control remains untested. 128

129 We hypothesize that different types of conflict are represented as points in a 130 cognitive space. The dimensions in the cognitive space of conflict can be the 131 aforementioned domains, in which domain-specific cognitive control processes are 132 defined. For a specific type of conflict, its location in the cognitive space can be 133 parameterized using a limited number of coordinates, which reflect how much control 134 is needed for each of the domain-specific cognitive control processes. The cognitive space can also represent different types of conflict with low dimensionality 26,31 . 135 Different domains can be represented conjunctively in a single cognitive space to 136 137 achieve domain-general cognitive control, as conflict from different sources can be resolved using the same set of cognitive control processes. We further hypothesize 138 that the cognitive space representing different types of conflict may be located in the 139 frontoparietal network due to its essential roles in conflict resolution^{20,32} and abstract 140 task representation³⁰. 141

In this study, we adjusted the paradigm from our previous study²⁸ by including 142 143 transitions of trials from five different conflict types, which enabled us to test if these 144 conflict types are organized in a cognitive space (Fig. 1A). Specifically, on each trial, 145 an arrow, pointing either upwards or downwards, was presented on one of the 10 possible locations on the screen. Participants were required to respond to the pointing 146 direction of the arrow (up or down) by pressing either the left or right key. 147 148 Importantly, conflict from two sources can occur in this task. On one hand, the 149 vertical location of the arrow can be incongruent with the direction (e.g., an uppointing arrow on the lower half of the screen), resulting spatial Stroop conflict^{6,33}. 150 On the other hand, the horizontal location of the arrow can be incongruent with the 151

response key (e.g., an arrow requiring left response presented on the right side of the screen), thus causing Simon conflict^{33,34}. As the arrow location rotates from the horizontal axis to the vertical axis, spatial Stroop conflict increases, and Simon conflict decreases. Therefore, the 10 possible locations of the arrow give rise to five conflict types with unique blend of spatial Stroop and Simon conflict²⁸. As the increase in spatial Stroop conflict is perfectly correlated with the decrease in Simon conflict, we can use a 1D cognitive space to represent all five conflict types.



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160 Fig. 1. Experimental design. (A) The left panel shows the orthogonal stimulus-response mappings of 161 the two participant groups. In each group the stimuli were only displayed at two quadrants of the 162 circular locations. One group were asked to respond with the left button to the upward arrow and with 163 the right button to the downward arrow presented in the to-left and bottom-right quadrants, and the 164 other group vice versa. The right panel shows the time course of one example trial. The stimuli were 165 displayed for 600 ms, preceded and followed by fixation crosses that lasted for 1400 ms in total. (B) 166 Examples of the five types of conflict, each containing congruent and incongruent conditions. The 167 arrows were presented at locations along five orientations with isometric polar angles, in which the 168 vertical location introduces the spatial Stroop conflict, and the horizontal location introduces the Simon 169 conflict. Dashed lines are shown only to indicate the location of arrows and were not shown in the 170 experiments. (C) The definition of the angular difference between two conflict types and the conflict 171 similarity. The angle θ is determined by the acute angle between two lines that cross the stimuli and the 172 central fixation. Therefore, stimuli of the same conflict type form the smallest angle of 0, and stimuli

173 between Conflict 1 and Conflict 5 form the largest angle of 90°, and others are in between. Conflict 174 similarity is defined by the cosine value of θ .

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176 One way to parameterize (i.e., defining a coordinate system) the cognitive space 177 is to encode each conflict type by the angle of the axis connecting its two possible 178 stimulus locations (Fig. 1B). Within this cognitive space, the similarity between two 179 conflict types can be quantified as the cosine value of their angular difference (Fig. 180 1C). If the conflict types are organized as a cognitive space in the brain, the similarity between conflict types in the cognitive space should be reflected in both the behavior 181 182 and similarity in the neural representations of conflict types. Our data from two 183 experiments using this experimental design support both predictions: using behavioral data, we found that the influence of congruency (i.e., whether the task-relevant and 184 185 task-irrelevant information indicate the same response) from the previous trial to the next trial increases with the conflict similarity between the two trials. Using fMRI 186 data, we found that more similar conflict showed higher multivariate pattern similarity 187 188 in the right dorsolateral prefrontal cortex (dlPFC).

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190 **Results**

191 Conflict type similarity modulated behavioral congruency sequence effect (CSE)

192 Experiment 1.

193 We conducted a behavioral experiment (n = 33, 18 females) to examine how CSEs 194 across different conflict types are influenced by their similarity. First, we validated the 195 experimental design by testing the congruency effects. All five conflict types showed 196 robust congruency effects such that the incongruent trials were slower and less 197 accurate than the congruent trials (Note S1; Fig. S1 A/B). To test the influence of 198 similarity between conflict types on behavior, we examined the CSE in consecutive 199 trials. Specifically, the CSE was quantified as the interaction between previous and 200 current trial congruency and can reflect how (in)congruency on the previous trial influences cognitive control on the current trial^{35,36}. It has been shown that the CSE 201 202 diminishes if the two consecutive trials have different conflict types³⁷⁻³⁹. Similarly, we 203 tested whether the size of CSE increases as a function of conflict similarity between 204 consecutive trials. To this end, we organized trials based on a 5 (previous trial conflict 205 type) \times 5 (current trial conflict type) \times 2 (previous trial congruency) \times 2 (current trial 206 congruency) factorial design, with the first two and the last two factors capturing 207 between-trial conflict similarity and the CSE, respectively. The cells in the 5×5 208 matrix were mapped to different similarity levels according to the angular difference 209 between the two conflict types (Fig. 1C). As shown in Fig. 2, the CSE, measured in 210 both reaction time (RT) and error rate (ER), scaled with conflict similarity. 211 To test the modulation of conflict similarity on the CSE, we constructed a linear 212 mixed effect model to predict RT/ER in each cell of the factorial design using a

213 predictor encoding the interaction between the CSE and conflict similarity (see

214 Methods). The results showed a significant effect of conflict similarity (RT: $\beta = 0.10$

215	± 0.01 , $t(1978) = 15.82$, $p < .001$, $\eta_p^2 = .120$; ER: $\beta = 0.15 \pm 0.02$, $t(1978) = 7.84$, $p < 0.01$
216	.001, $\eta_p^2 = .085$, Fig. S2B/E). In other words, the CSE increased with the conflict
217	similarity between two consecutive trials. The conflict similarity modulation effect
218	remained significant after regressing out the influence of physical proximity between
219	the stimuli of consecutive trials (Note S2). As a control analysis, we also compared
220	this approach to a two-stage analysis that first calculated the CSE for each previous \times
221	current trial conflict type condition and then tested the modulation of conflict
222	similarity on the CSEs ²⁸ . The two-stage analysis also showed a strong effect of
223	conflict similarity (RT: $\beta = 0.58 \pm 0.04$, $t(493) = 14.74$, $p < .001$, $\eta_p^2 = .383$; ER: $\beta =$
224	0.36 ± 0.05 , $t(493) = 7.01$, $p < .001$, $\eta_p^2 = .321$, Fig. S2A/D). Importantly, individual
225	modulation effects of conflict similarity were positively correlated between the two
226	approaches (RT: $r = 0.48$; ER: $r = 0.86$, both $ps < 0.003$, one-tailed), indicating the
227	consistency of the estimated conflict similarity effects across the two approaches.



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Fig. 2. The conflict similarity modulation on the behavioral CSE in Experiment 1. (A) RT and (B)
 ER are plotted as a function of congruency types on trial n-1 and trial n. Each column shows one

similarity level, as indicated by the defined angular difference between two conflict types. Error bars
are standard errors. C = congruent; I = incongruent; RT = reaction time; ER = error rate.

- 233
- Experiment 2.

235 Behavioral results. We next conducted an fMRI experiment using a shorter version of

236 the same task with a different sample (n = 35, 17 females) to seek neural evidence of

how different conflict types are organized. Using behavioral data, we first validated

the experimental design by testing congruency effects in each of the five conflict

- types (Note S1; Fig. S1 C/D). We then tested the modulation of conflict similarity on the behavioral CSE using the linear mixed effect model as in Experiment 1 (except the two-stage method). Results showed a significant effect of conflict similarity modulation (RT: $\beta = 0.24 \pm 0.04$, t(1148) = 6.36, p < .001, $\eta_p^2 = .096$; ER: $\beta = 0.33 \pm$ 0.06, t(1206) = 5.81, p < .001, $\eta_p^2 = .124$, Fig. S2C/F), thus replicating the results of Experimental 1 and setting the stage for fMRI analysis. As in Experiment 1, the conflict similarity modulation effect remained significant after regressing out the
- 246 influence of physical proximity between the stimuli of consecutive trials (Note S2).
- 247 Brain activations modulated by conflict type dissimilarity with univariate analyses



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249Fig. 3. The congruency effect and parametric modulation effect detected by uni-voxel analyses.250Results displayed are thresholded with voxel-wise one-tailed p < .005 and cluster-size > 20 voxels. The

251 congruency effect denotes the higher activation in incongruent than congruent condition. The positive 252 parametric modulation effect ($I_pm - C_pm$) denotes the higher activation when the conflict type 253 contained a higher ratio of Simon conflict component (bottom left panel). The negative parametric 254 modulation effect [converted to positive with - ($I_pm - C_pm$)] denotes the higher activation when the 255 conflict type contained a higher ratio of spatial Stroop conflict component (bottom right panel). I = 256 incongruent; C = congruent; pm = parametric modulator.

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In the fMRI analysis, we first replicated the classic congruency effect by searching for

brain regions showing higher univariate activation in incongruent than congruent $\frac{2040}{10}$ and \frac

260 conditions (GLM1, see Methods). Consistent with the literature 20,40 , this effect was

261 observed in the pre-supplementary motor area (pre-SMA) and anterior cingulate

cortex (ACC) areas (Fig. 3, Table S1). We then tested the encoding of conflict type as

a cognitive space by identifying brain regions with activation levels parametrically 263 264 covarying with the coordinates (i.e., axial angle relative to the horizontal axis) in the 265 hypothesized cognitive space. As shown in Fig. 1B, change in the angle corresponds 266 to change in spatial Stroop and Simon conflicts in opposite directions. Accordingly, in 267 the left middle frontal gyrus (MFG), fMRI activation scaled with the increase in 268 spatial Stroop conflict, whereas the right inferior parietal sulcus (IPS) and the right 269 dorsomedial prefrontal cortex (dmPFC) displayed positive correlation between fMRI 270 activation and Simon conflict (Fig. 3, Fig. S3, Table S1).

271 To further test if the univariate results explain the conflict similarity modulation 272 of the behavioral CSE (slope in Fig. S2C), we conducted brain-behavioral correlation 273 analyses for regions identified above. Regions with higher spatial Stroop/Simon 274 modulation effects were expected to trigger higher behavioral conflict similarity 275 modulation effect on the CSE. However, none of the three regions (i.e., left MFG, 276 right IPS and right dmPFC, Fig. 3) were positively correlated with the behavioral 277 performance, all $p_{FDR} > .762$, one-tailed. In addition, since the conflict type difference 278 covaries with the orientation of the arrow location at the individual level (e.g., the 279 stimulus in a higher level of Simon conflict is always closer to the horizontal axis, see 280 Fig. S4), the univariate modulation effects may not reflect purely conflict type difference. To further tease these factors apart, we used multivariate analyses. 281

282 Multivariate patterns of the right dlPFC encodes the conflict similarity





Fig. 4. The conflict type effect. (A) Brain regions surviving the FDR-correction ($p_{FDR} < 0.05$ and p < 0.001) across the 360 regions (criterion 1). Labeled regions are those meeting the criterion 2. (B) The regions showing stronger encoding of conflict type in the incongruent than congruent conditions

- 287 (criterion 2). ** $p_{FDR} < .01$, *** $p_{FDR} < .001$. (C) The brain-behavior correlation of the right 8C 288 (criterion 3). (D) Illustration of the different encoding strength of conflict type similarity in incongruent 289 versus congruent conditions of right 8C. 1 = left; r = right.
- 290

291 The hypothesis that the brain encodes conflict types in a cognitive space predicts that 292 similar conflict types will have similar neural representations. To test this prediction, 293 we computed the representational similarity matrix (RSM) that encoded correlations 294 of blood-oxygen-level dependent (BOLD) signal patterns between each pair of 295 conflict type (conflict 1, 2, 3, 4 and 5, as shown in Fig. 1B) \times congruency (congruent, 296 incongruent) \times arrow direction (up, down) \times run \times subject combinations for each of the 360 cortical regions from the Multi-Modal Parcellation (MMP) cortical atlas^{41,42}. 297 298 The RSM was then submitted to a linear mixed-effect model as the dependent 299 variable to test whether the representational similarity in each region was modulated 300 by various experimental variables (e.g., conflict type, spatial orientation, stimulus, 301 response, etc., see Methods). The linear mixed-effect model was used to de-correlate 302 conflict type and spatial orientation leveraging the between-subject manipulation of 303 stimulus locations (Fig. S4).

304 To validate this method, we applied this analysis to test the effects of response/stimulus features and found that representational similarity of the BOLD 305 306 signal significantly covaried with whether two response/spatial location/arrow 307 directions were the same most strongly in bilateral motor/visual/somatosensory areas, 308 respectively (Fig. S5). We then identified the cortical regions encoding conflict type 309 as a cognitive space by testing whether their RSMs can be explained by the similarity 310 between conflict types. Specifically, we applied three independent criteria: (1) the 311 cortical regions should exhibit a statistically significant positive conflict similarity 312 effect on the RSM; (2) the conflict similarity effect should be stronger in incongruent 313 than congruent trials to reflect flexible adjustment of cognitive control demand when 314 conflict is present; and (3) the conflict similarity effect should be positively correlated 315 with the behavioral conflict similarity modulation effect on the CSE (see Behavioral 316 *Results* of Experiment 2). The first criterion revealed several cortical regions encoding 317 the conflict similarity, including the 8C area (a subregion of dlPFC⁴²), a47r, TPOJ3 and V3CD in the right hemisphere, and the 6r, 7Am, 24dd, VMV1, VMV2, 7Pl, 23c 318 319 and 25 areas in the left hemisphere ($p_{FDR}s < 0.05$, with raw ps < 0.001, one-tailed, Fig. 320 4A). We next tested whether these regions were related to cognitive control by 321 comparing the strength of conflict similarity effect between incongruent and 322 congruent conditions (criterion 2). Results revealed that the left lateral area 7P (7P1), 323 left ventromedial visual area 1 (VMV1), left dorsal area 24d (24dd), right Brodmann 324 area 8C (8C), and right V3CD met this criterion, p_{FDR} s < .01, one-tailed (Table 1, Fig. 325 4B), suggesting that the representation of conflict type was strengthened when 326 conflict was present (e.g., Fig. 4D). The inter-subject brain-behavioral correlation 327 analysis (criterion 3) showed that the strength of conflict similarity effect on RSM 328 scaled with the modulation of conflict similarity on the CSE (slope in Fig. S2C) in 329 right 8C (r = 0.43, $p_{FDR} = .027$, one-tailed, Fig. 4C) but not in the other regions (all 330 $p_{FDR} > .632$, one-tailed). In addition, we did not find evidence supporting the encoding

- 331 of congruency in the right 8C area (see Note S5), suggesting that the right 8C area
- 332 specifically represents conflict similarity. In sum, we found converging evidence
- 333 supporting that the right dIPFC (8C area) encoded conflict similarity, which further
- 334 supports the hypothesis that conflict types are represented in a cognitive space.

335 Multivariate patterns of visual and oculomotor areas encode stimulus orientation



Fig. 5. The axial orientation effect. (A) Brain regions surviving the FDR-correction ($p_{FDR} < 0.05$ and p < 0.001) across the 360 regions (criterion 1). Labeled regions are those meeting the criterion 2. (B) The regions showing stronger encoding of orientation in the incongruent than congruent conditions (criterion 2). * $p_{FDR} < .05$, ** $p_{FDR} < .01$, *** $p_{FDR} < .001$.

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342 To tease apart the representation of conflict type from that of perceptual information, 343 we tested the modulation of the spatial orientations of stimulus locations on RSM 344 using the aforementioned RSA. We also applied three independent criteria: (1) the cortical regions should exhibit a statistically significant orientation effect on the RSM; 345 346 (2) the conflict similarity effect should be stronger in incongruent than congruent 347 trials; and (3) the orientation effect should not interact with the CSE, since the 348 orientation effect was dissociated from the conflict similarity effect and was not 349 expected to influence cognitive control. We observed increasing fMRI 350 representational similarity between trials with more similar orientations of stimulus 351 location in the occipital cortex, such as right V1, bilateral V2 and V3, right V4, left 352 area temporoparietooccipital junction 3 (TPOJ3) and right PHT areas (FDR corrected 353 ps < 0.05 and raw ps < 0.001). We also found the same effect in several oculomotor 354 related regions, including the left frontal eye field (FEF), anterior 6m (6ma), area 355 intraparietal 2 (IP2), right parietal area F (PF) and bilateral 5m, as well as other 356 regions (Fig. 5A). Then we tested if any of these brain regions were related to the 357 conflict representation by comparing their encoding strength between incongruent and 358 congruent conditions. Results showed that the right V1, bilateral V2, left FEF, left 359 IP2, right hippocampus (H) and right PF encoded stronger orientation effect in the 360 incongruent than the congruent condition, $p_{FDRS} < .05$, one-tailed (Table 1, Fig. 5B). 361 We then tested if any of these regions was related to the behavioral performance, and 362 results showed that none of them positively correlated with the behavioral conflict 363 similarity modulation effect, all $p_{FDR} > .675$, one-tailed. Thus all regions are 364 consistent with the criterion 3. Like the right 8C area, none of the reported areas directly encoded congruency (see Note S5). Taken together, we found that the visual 365

and oculomotor regions encoded orientations of stimulus location in a continuousmanner and that the encoding strength was stronger when conflict was present.

To explore the relation between conflict type and orientation representations, we 368 369 conducted representational connectivity (i.e., the similarity between two RSMs of two regions)⁴³ analyses and found that among the orientation effect regions, the right V1 370 371 and bilateral V2 showed significant representational connectivity with the right 8C 372 compared to the controlled regions (including those encoding orientation effect but 373 not showing larger encoding strength in incongruent than congruent conditions, as 374 well as three other regions encoding none of our defined effects in the main RSA, see 375 Methods). Compared with the largest connectivity strength in the controlled regions (i.e., the left V3, $\beta = 0.1447 \pm 0.0069$), we found higher connectivity in the left V2, β 376 377 $= 0.1645 \pm 0.0060$, t(34) = 4.86, right V1, $\beta = 0.1628 \pm 0.0065$, t(34) = 4.54, and 378 right V2, $\beta = 0.1678 \pm 0.0074$, t(34) = 5.65, all $p_{FDR} < .001$, one-tailed (Fig. S6).

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Table 1. Summary statistics of regions showing larger encoding strength in
 incongruent than congruent conditions for the conflict type and

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orientation effects.				
Region name	<i>t</i> (34)	β (SD)	Cohen's d	$p_{\rm FDR}$
		Conflict type effect		
left 7P1	3.13	0.0049 ± 0.0016	0.53	.011
left VMV1	3.96	0.0077 ± 0.0019	0.67	.002
left 24	7.82	0.0094 ± 0.0012	1.32	< .001
right 8C	3.15	0.0073 ± 0.0023	0.53	.011
right V3CD	2.86	0.0057 ± 0.0020	0.48	.017
		Orientation effect		
left V2	3.20	0.0107 ± 0.0033	0.54	.007
left FEF	2.97	0.0066 ± 0.0022	0.50	.010
left IP2	5.73	0.0129 ± 0.0022	0.97	.001
right V1	2.70	0.0060 ± 0.0022	0.46	.014
right V2	3.26	0.0083 ± 0.0025	0.55	.007
right H	2.79	0.0037 ± 0.0013	0.47	.014
right PF	5.31	0.0097 ± 0.0018	0.90	< .001

383

384 **Discussion**

385	Understanding how different types of conflict are resolved is essential to answer how
386	cognitive control achieves adaptive behavior. However, the dichotomy between
387	domain-general and/or domain-specific processes presents a dilemma ^{15,21} .
388	Reconciliation of the two views also suffers from the inability to fully address how
389	infinite conflict can be resolved by a limited set of cognitive control processes. In this
390	study, we hypothesized that this issue can be addressed if conflict is organized as a
391	cognitive space. Leveraging the well-known dissociation between the spatial Stroop
392	and Simon conflict ⁴⁴⁻⁴⁶ , we designed five conflict types that are systematically

393 different from each other. The cognitive space hypothesis predicted that the 394 representational proximity/distance between two conflict types scales with their 395 similarities/dissimilarities, which was tested at both behavioral and neural levels. 396 Behaviorally, we found that the CSEs were linearly modulated by conflict similarity between consecutive trials, replicating and extending our previous study²⁸, BOLD 397 398 activity patterns in the right dIPFC further showed that the representational similarity 399 between conflict types was modulated by their conflict similarity, and that strength of 400 the modulation was positively associated with the modulation of conflict similarity on the behavioral CSE. We also observed that activity in three brain regions (right IPS, 401 402 right dlPFC and left MFG) was parametrically modulated by the conflict type 403 difference, though they did not directly explain the behavioral results. Additionally, 404 we found that the visual regions encoded the spatial orientation of the stimulus 405 location, which might provide the essential concrete information to determine the 406 conflict type. Together, these results support the hypothesis that the conflicts are 407 organized in a cognitive space that enables a limited set of cognitive control processes

408 to resolve infinite possible types of conflict.



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410 Fig. 6. Illustration of the hypothesized dimensionalities of different representations. The shade of 411 the red color indicates the degree of dimensionality (i.e., how many dimensions are needed to represent 412 different states). The dimensionality of domain-general representation is extremely low, with all 413 representations compressed to one dot. The dimensionality of domain-specific representation is 414 extremely high, with each control state encoded in a unique and orthogonal dimension. The 415 dimensionality of the organized representation is modest, enabling distant states to be separated but 416 also allowing close states to share representations. The solid arrows show the axes of different

- 417 dimensions. The dashed arrows indicate how the representational dimensionality can be reduced by
- 418 projecting the independent dimensions to a common dimension.
- 419

420 Conventionally, the domain-general view of control suggests a common

- 421 representation for different types of conflict (Fig. 6, left), while the domain-specific
- 422 view suggests dissociated representations for different types (Fig. 6, right). Previous
- 423 research on this topic often adopts a binary manipulation of conflict²¹ (i.e., each
- 424 domain only has one conflict type) and thus is not suitable to test the cognitive space

hypothesis. Here, we parametrically manipulated the similarity of conflict in different 425 426 conflict types and demonstrated that the two theories can be reconciled as a cognitive $space^{22}$ (Fig. 6, middle). Specifically, the cognitive space provides a solution to use a 427 single cognitive space organization to encode different types of conflict that are close 428 429 (domain-general) or distant (domain-specific) to each other. It also shows the 430 potential for how unlimited conflict types can be coded using limited resources (i.e., 431 as different points in a low-dimensional cognitive space). Moreover, geometry can also emerge in the cognitive space²⁰, which will allow for decomposition of a conflict 432 type (e.g., how much conflict in each of the dimensions in the cognitive space) so that 433 434 it can be mapped into the limited set of cognitive control processes. Such geometry 435 enables fast learning of cognitive control settings from similar conflict types by 436 providing a measure of similarity (e.g., as distance in space).

437 If the dimensionality of the cognitive space of conflict is extremely high, the 438 cognitive space solution would suffer the same criticism as the domain-specificity 439 theory. We argue that the dimensionality is manageable for the human brain, as task information unrelated to differentiating conflicts can be removed. For example, the 440 441 Simon conflict can be represented in a space consisting of spatial location, stimulus 442 information and responses. Thus, the dimensionality of the cognitive space of conflict should not exceed the number of represented features. The dimensionality can be 443 444 further reduced, as humans selectively represent a small number of features when learning task representations (e.g., spatial information is reduced to the horizontal 445 dimension from the 3D space we live in)⁴⁷. The reduced dimensionality does not only 446 require less effort to represent the conflict, but also facilitates generalization of 447 448 cognitive control settings among different conflict types²⁶.

Although our finding of cognitive space in the right dlPFC differs from other 449 cognitive space studies^{24,25,48} that highlighted the orbitofrontal and hippocampus 450 regions, it is consistent with the cognitive control literature. The prefrontal cortex has 451 long been believed to be a key region of cognitive control representation⁴⁹⁻⁵¹ and is 452 widely engaged in multiple task demands^{12,52}. However, it is not until recently that the 453 multivariate representation in this region has been examined. For instance, Vaidva et 454 455 al.²⁹ reported that frontal regions presented latent states that are organized hierarchically. Freund et al.³² showed that dIPFC encoded the target and congruency 456 in a typical color-word Stroop task. Taken together, we suggest that the right dlPFC 457 458 might flexibly encode a variety of cognitive spaces to meet the dynamic task 459 demands. In addition, we found no such representation in the left dlPFC (Note S6), 460 indicating a possible lateralization. Previous studies showed that the left dIPFC was related to the expectancy-related attentional set up-regulation, while the right dlPFC 461 was related to the online adjustment of control^{53,54}, which is consistent with our 462 findings. Moreover, the right PFC also represents a composition of single rules⁵⁵, 463 which may explain how the spatial Stroop and Simon types can be jointly encoded in 464 465 a single space.

We found that participants with stronger conflict representation as cognitive
space in right dlPFC have also adjusted their conflict control to a greater extent based
on the conflict similarity (Fig 4C). The finding suggests that the cognitive space

469 organization of conflict guides cognitive control to adjust behavior. Previous studies 470 have shown that participants may adopt different strategies to represent a task, with the model-based strategies benefitting goal-related behaviors more than the model-471 free strategies⁵⁶. Similarly, we propose that the cognitive space could serve as a 472 mental model to assist fast learning and efficient organization of cognitive control 473 474 settings. With the organization of a cognitive space, a new conflict can be quickly 475 assigned a location in the cognitive space, which will facilitate the development of 476 cognitive control settings for this conflict by interpolating nearby conflicts and/or 477 projecting the location to axes representing different cognitive control processes. On 478 the other hand, without a cognitive space, there would be no measure of similarity 479 between conflict on different trials, hence limiting the ability of fast learning of 480 cognitive control setting from similar trials.

481 The cognitive space in the right dIPFC appears to be an abstraction of concrete 482 information from the visual regions. We found that the right V1 and bilateral V2 483 encoded the spatial orientation of the target location (Fig. 5) and showed strong representational connectivity with the right dlPFC (Fig. S6), suggesting that there 484 485 might be information exchange between these regions. We speculate that the 486 representation of spatial orientation may have provided the essential perceptual information to determine the conflict type (Fig. 1) and thus served as the critical input 487 488 for the cognitive space. The conflict type representation further incorporates the 489 stimulus-response mapping rules to the spatial orientation representation, so that 490 vertically symmetric orientations can be recognized as the same conflict type (Fig. 491 S4). In other words, the representation of conflict type involves the compression of perceptual information⁵⁷, which is consistent with the idea of a low-dimensional 492 representation of cognitive control^{26,31}. The compression and abstraction processes 493 might be why the frontoparietal regions are the top of hierarchy of information 494 495 processing⁵⁸ and why the frontoparietal regions are widely engaged in multiple task demands⁵⁹. 496

497 With conventional univariate analyses, we observed that the overall congruency effect was located at the medial frontal regions (i.e., pre-SMA and ACC), which is 498 consistent with previous studies 20,40 . Beyond that, we also found regions that can be 499 parametrically modulated by conflict type difference, including right IPS, right dlPFC 500 (modulated by Simon difference) and left MFG (modulated by spatial Stroop 501 502 difference). The lateralization of these regions is consistent with a previous finding¹⁹, 503 which highlighted the difference of Stroop and Simon types with brain activities at 504 different hemispheres. The scaling of brain activities based on conflict difference is 505 potentially important to the representational organization of different types of conflict. 506 However, we didn't observe their brain-behavioral relevance. One possible reason is 507 that the conflict (dis)similarity is a combination of (dis)similarity of spatial Stroop and 508 Simon conflicts, but each univariate region only reflects difference along a single conflict domain. Also likely, the representational geometry is more of a multivariate 509 problem than what univariate activities can capture⁶⁰. Future studies may adopt 510 511 approaches such as repetition suppression induced fMRI adaptation²⁶ to test the role 512 of univariate activities in task representations.

513 One limitation of this study needs to be noted. To parametrically manipulate the 514 conflict similarity levels, we adopted the spatial Stroop-Simon paradigm that enables 515 parametrical combinations of spatial Stroop and Simon conflicts. However, since this 516 paradigm is a two-alternative forced choice design, the behavioral CSE is not a pure 517 measure of adjusted control but could be partly confounded by bottom-up factors such 518 as feature integration⁶¹. Future studies may replicate our findings with a multiple-519 choice design with confound-free trial sequences⁶².

In sum, we showed that the cognitive control can be organized in an abstract cognitive space that is represented in the right dlPFC and guides cognitive control to adjust goal-directed behavior. The cognitive space hypothesis reconciles the longstanding debate between the domain-general and domain-specific views of cognitive control and provides a parsimonious and more broadly applicable framework for understanding how our brains efficiently and flexibly represents multiple task settings.

527

528

529 Materials and Methods

530 Subjects

531 In Experiment 1, we enrolled thirty-three college students (19-28 years old, average of

532 21.5 ± 2.3 years old; 19 males). In Experiment 2, thirty-six college students were

533 recruited, and one subject was excluded due to not following task instructions. The

final sample of Experiment 2 consisted of thirty-five participants (19-29 years old,

average of 22.3 ± 2.5 years old; 17 males). The sample sizes were determined based on our previous study²⁸. All participants reported no history of psychiatric or

on our previous study²⁸. All participants reported no history of psychiatric or
 neurological disorders and were right-handed, with normal or corrected-to-normal

538 vision. The experiments were approved by the Institutional Review Board of the

- 539 Institute of Psychology, Chinese Academy of Science. Informed consent was obtained
- 540 from all subjects.
- 541

542 Method Details

543 Experiment 1

544 *Experimental Design*. We adopted a modified spatial Stroop-Simon task²⁸ (Fig. 1).

545 The task was programmed with the E-prime 2.0 (Psychological Software Tools, Inc.).

546 The stimulus was an upward or downward black arrow (visual angle of ~ 1°)

547 displayed on a 17-inch LCD monitor with a viewing distance of ~60 cm. The arrow

548 appeared inside a grey square at one of ten locations with the same distance from the

549 center of the screen, including two horizontal (left and right), two vertical (top and

bottom), and six corner (orientations of 22.5° , 45° and 67.5°) locations. The distance

from the arrow to the screen center was approximately 3°. To dissociate orientation of

stimulus locations and conflict types (see below), participants were randomly
assigned to two sets of stimulus locations (one included top-right and bottom-left
quadrants, and the other included top-left and bottom-right quadrants).

555 Each trial started with a fixation cross displayed in the center for 100–300 ms, 556 followed by the arrow for 600 ms and another fixation cross for 1100-1300 ms (the 557 total trial length was fixed at 2000 ms). Participants were instructed to respond to the 558 pointing direction of the arrow by pressing a left or right button and to ignore its 559 location. The mapping between the arrow orientations and the response buttons was counterbalanced across participants. The task design introduced two possible sources 560 of conflict: on one hand, the direction of the arrow is either congruent or incongruent 561 with the vertical location of the arrow, thus introducing a spatial Stroop conflict 33,63 . 562 563 which contains the dimensional overlap between task-relevant stimulus and task-564 irrelevant stimulus¹; on the other hand, the response (left or right button) is either congruent or incongruent with the horizontal location of the arrow, thus introducing a 565 Simon conflict^{33,34}, which contains the dimensional overlap between task-irrelevant 566 stimulus and response¹. Therefore, the five polar orientations of the stimulus location 567 568 (from 0 to 90°) defined five unique combinations of spatial Stroop and Simon 569 conflicts, with more similar orientations having more similar composition of conflict. More generally, the spatial orientation of the arrow location relative to the center of 570 571 the screen forms a cognitive space of different blending of spatial Stroop and Simon 572 conflict.

573 The formal task consisted of 30 runs of 101 trials each, divided into three sessions 574 of ten runs each. The participants completed one session each time and all three 575 sessions within one week. Before each session, the participants performed training 576 blocks of 20 trials repeatedly until the accuracy reached 90% in the most recent block. 577 The trial sequences of the formal task were pseudo-randomly generated to ensure that 578 each of the task conditions and their transitions occurred with equal number of trials.

579 Experiment 2

580 *Experimental Design*. The apparatus, stimuli and procedure were identical to

581 Experiment 1 except for the changes below. The stimuli were back projected onto a

screen (with viewing angle being $\sim 3.9^{\circ}$ between the arrow and the center of the

screen) behind the subject and viewed via a surface mirror mounted onto the head

584 coil. Due to the time constraints of fMRI scanning, the trial numbers decreased to a

total of 340, divided into two runs with 170 trials each. To obtain a better

hemodynamic model fitting, we generated two pseudo-random sequences optimized with a genetic algorithm⁶⁴ conducted by the NeuroDesign package⁶⁵ (see Note S3 for more detail). In addition, we added 6 seconds of fixation before each run to allow the stabilization of the hemodynamic signal, and 20 seconds after each run to allow the signal to drop to the baseline.

591 Before scanning, participants performed two practice sessions. The first one 592 contained 10 trials of center-displayed arrow and the second one contained 32 trials 593 using the same design as the main task. They repeated both sessions until their 594 performance accuracy for each session reached 90%, after which the scanning began.

595 fMRI Image acquisition and preprocessing

596 Functional imaging was performed on a 3T GE scanner (Discovery MR750) using 597 echo-planar imaging (EPI) sensitive to BOLD contrast [in-plane resolution of $3.5 \times 3.5 \text{ mm}^2$, 64×64 matrix, 37 slices with a thickness of 3.5 mm and no interslice skip, 598 repetition time (TR) of 2000 ms, echo-time (TE) of 30 ms, and a flip angle of 90°]. In 600 addition, a sagittal T1-weighted anatomical image was acquired as a structural 601 reference scan, with a total of 256 slices at a thickness of 1.0 mm with no gap and an 602 in-plane resolution of $1.0 \times 1.0 \text{ mm}^2$.

603 Before preprocessing, the first three volumes of the functional images were 604 removed due to the instability of the signal at the beginning of the scan. The

anatomical and functional data were preprocessed with the fMRIprep $20.2.0^{66}$

606 (RRID:SCR_016216), which is based on Nipype $1.5.1^{67}$ (RRID:SCR_002502).

607 Specifically, BOLD runs were slice-time corrected using 3dTshift from AFNI

608 20160207⁶⁸ (RRID:SCR_005927). The BOLD time-series were resampled to the

609 MNI152NLin2009cAsym space without smoothing. For a more detailed description

610 of preprocessing, see Note S4. After preprocessing, we resampled the functional data 611 to a spatial resolution of $3 \times 3 \times 3$ mm³. All analyses were conducted in volumetric

611 to a spatial resolution of $3 \times 3 \times 3$ mm³. All analyses were conducted in 612 space, and surface maps are produced with Connectome Workbench

613 (https://www.humanconnectome.org/software/connectome-workbench) for display

- 614 purpose only.
- 615 *Quantification and Statistical Analysis*

616 Behavioral analysis

617 *Experiment 1.* RT and ER were the two dependent variables analyzed. As for RTs, 618 we excluded the first trial of each block (0.9%, for CSE analysis only), error trials 619 (3.8%), trials with RTs beyond three SDs or shorter than 200 ms (1.3%) and post-620 error trials (3.4%). For the ER analysis, the first trial of each block and trials after an error were excluded. To exclude the possible influence of response repetition, we 621 622 centered the RT and ER data within the response repetition and response alternation 623 conditions separately by replacing condition-specific mean with the global mean for 624 each subject.

625 To examine the modulation of conflict similarity on the CSE, we organized trials based on a 5 (previous trial conflict type) \times 5 (current trial conflict type) \times 2 (previous 626 trial congruency) \times 2 (current trial congruency) factorial design. As conflict similarity 627 is commutive between conflict types, we expected the previous by current trial 628 629 conflict type factorial design to be a symmetrical (e.g., a conflict 1-conflict 2 630 sequence in theory has the same conflict similarity modulation effect as a conflict 2-631 conflict 1 sequence), resulting a total of 15 conditions left for the first two factors of 632 the design (i.e., previous \times current trial conflict type). For each previous \times current 633 trial conflict type condition, the conflict similarity between the two trials can be quantified as the cosine of their angular difference. In the current design, there were 634 five possible angular difference levels $(0, 22.5^{\circ}, 42.5^{\circ}, 67.5^{\circ} \text{ and } 90^{\circ}, \text{ see Fig. 1C})$. 635

We further coded the previous by current trial congruency conditions (hereafter 636 abbreviated as CSE conditions) as CC, CI, IC and II, with the first and second letter 637 638 encoding the congruency (C) or incongruency (I) on the previous and current trial, 639 respectively. As the CSE is operationalized as the interaction between previous and 640 current trial congruency, it can be rewritten as a contrast of (CI - CC) - (II - IC). In 641 other words, the load of CSE on CI, CC, II and IC conditions is 1, -1, -1 and 1, -1642 respectively. To estimate the modulation of conflict similarity on the CSE, we built a 643 regressor by calculating the Kronecker product of the conflict similarity scores of the 644 15 previous \times current trial conflict similarity conditions and the CSE loadings of 645 previous × current trial congruency conditions. This regressor was regressed against 646 RT and ER data separately, which were normalized across participants and CSE 647 conditions. The regression was performed using a linear mixed-effect model, with the 648 intercept and the slope of the regressor for the modulation of conflict similarity on the CSE as random effects (across both participants and the four CSE conditions). As a 649 control analysis, we built a similar two-stage model²⁸. In the first stage, the CSE [i.e., 650 (CI - CC) - (II - IC) for each of the previous × current trial conflict similarity 651 652 condition was computed. In the second stage, CSE was used as the dependent variable 653 and was predicted using conflict similarity across the 15 previous \times current trial conflict type conditions. The regression was also performed using a linear mixed 654 655 effect model with the intercept and the slope of the regressor for the modulation of 656 conflict similarity on the CSE as random effects (across participants). Experiment 2. Behavioral data was analyzed using the same linear mixed effect model 657 as Experiment 1, with all the CC, CI, IC and II trials as the dependent variable. In 658 659 addition, to test if fMRI activity patterns may explain the behavioral representations 660 differently in congruent and incongruent conditions, we conducted the same analysis to measure behavioral modulation of conflict similarity on the CSE using congruent 661 662 (CC and IC) and incongruent (CI and II) trials separately.

663 Estimation of fMRI activity with univariate general linear model (GLM)

664 To estimate voxel-wise fMRI activity for each of the experimental conditions, the preprocessed fMRI data of each run were analyzed with the GLM. We conducted 665 three GLMs for different purposes. GLM1 aimed to validate the design of our study 666 by replicating the engagement of frontoparietal activities in conflict processing 667 documented in previous studies^{7,19}, and to explore the cognitive space related regions 668 that were parametrically modulated by the conflict type. Preprocessed functional 669 670 images were smoothed using a 6-mm FWHM Gaussian kernel. We included 671 incongruent and congruent conditions as main regressors and appended a parametric 672 modulator for each condition. The modulation parameters for Conf 1, Conf 2, Conf 3, 673 Conf 4, and Conf 5 trials were -2, -1, 0, 1 and 2, respectively. In addition, we also 674 added event-related nuisance regressors, including error/missed trials, outlier trials 675 (slower than three SDs of the mean or faster than 200 ms) and trials within two TRs of significant head motion (i.e., outlier TRs, defined as standard DVARS > 1.5 or FD 676 > 0.9 mm from previous TR)⁴¹. On average there were 1.2 outlier TRs for each run. 677 These regressors were convolved with a canonical hemodynamic response function 678

679 (HRF) in SPM 12 (http://www.fil.ion.ucl.ac.uk/spm). We further added volume-level nuisance regressors, including the six head motion parameters, the global signal, the 680 white matter signal, the cerebrospinal fluid signal, and outlier TRs. Low-frequency 681 682 signal drifts were filtered using a cutoff period of 128 s. The two runs were regarded 683 as different sessions and incorporated into a single GLM to get more power. This 684 yielded two beta maps (i.e., a main effect map and a parametric modulation map) for 685 the incongruent and congruent conditions, respectively and for each subject. At the 686 group level, paired t-tests were conducted between incongruent and congruent conditions, one for the main effect and the other for the parametric modulation effect. 687 Since the spatial Stroop and Simon conflict change in the opposite direction to each 688 other, a positive modulation effect would reflect a higher brain activation when there 689 690 is more Simon conflict, and a negative modulation effect would reflect a higher brain 691 activation for more spatial Stroop conflict. To avoid confusion, we converted the 692 modulation effect of spatial Stroop to positive by using a contrast of [-(I pm -693 C pm)] throughout the results presentation. Results were thresholded by 3dclust function in AFNI ⁶⁹ with voxel-wise p < .005 and cluster-size > 20 voxels, which was 694 supposed to produce a desirable balance between Type I and II error rates⁷⁰. To 695 696 visualize the parametric modulation effects, we conducted a similar GLM (GLM2), 697 except we used incongruent and congruent conditions from each conflict type as separate regressors with no parametric modulation. Then we extracted beta 698 699 coefficients for each regressor and each participant with regions observed in GLM1 as 700 regions of interest, and finally got the incongruent-congruent contrasts for each 701 conflict type at the individual level. We reported the results in Fig. 3, Table S1, and Fig. S3. Visualization of the uni-voxel results was made by the MRIcron 702 703 (https://www.mccauslandcenter.sc.edu/mricro/mricron/).

704 The GLM3 aimed to prepare for the representational similarity analysis (see 705 below). There were several differences compared to GLM1. The unsmoothed functional images after preprocessing were used. This model included 20 event-706 707 related regressors, one for each of the 5 (conflict type) \times 2 (congruency condition) \times 2 708 (arrow direction) conditions. The event-related nuisance regressors were similar to 709 GLM1, but with additional regressors of response repetition and post-error trials to account for the nuisance inter-trial effects. To fully expand the variance, we 710 711 conducted one GLM analysis for each run. After this procedure, a voxel-wise fMRI 712 activation map was obtained per condition, run and subject.

713 Representational similarity analysis (RSA)

To measure the neural representation of conflict similarity, we adopted the RSA.

715 RSAs were conducted on each of the 360 cortical regions of a volumetric version of

the MMP cortical atlas⁴². To de-correlate the factors of conflict type and orientation of

stimulus location, we leveraged the between-subject manipulation of stimulus

718 locations and conducted RSA in a cross-subject fashion (Fig. S4)^{60,71}. The beta

- r19 estimates from GLM3 were noise-normalized by dividing the original beta
- 720 coefficients by the square root of the covariance matrix of the error terms⁷². For each
- 721 cortical region, we calculated the Pearson's correlations between fMRI activity

patterns for each run and each subject, yielding a 1400 (20 conditions \times 2 runs \times 35 722 723 participants) \times 1400 RSM. The correlations were calculated in a cross-voxel manner 724 using the fMRI activation maps obtained from GLM3 described in the previous 725 section. Similar to the behavioral analyses, we assumed the conflict similarity 726 between two trials is commutive and hence collapsed the RSM along the diagonal and 727 converted the lower triangle into a vector, which was then z-transformed and 728 submitted to a linear mixed effect model as the dependent variable. The linear mixed 729 effect model also included regressors of conflict similarity and orientation similarity. 730 Importantly, conflict similarity was based on how Simon and spatial Stroop conflict 731 are combined and hence was calculated by first rotating all subject's stimulus location 732 to the top-right and bottom-left quadrants, whereas orientation was calculated using 733 original stimulus locations. As a result, the regressors representing conflict similarity 734 and orientation similarity were de-correlated. Similarity between two conditions was 735 measured as the cosine value of the angular difference. Other regressors included a 736 target similarity regressor (i.e., whether the arrow directions were identical), a response similarity regressor (i.e., whether the correct responses were identical); a 737 738 spatial Stroop distractor regressor (i.e., vertical distance between two stimulus 739 locations); a Simon distractor regressor (i.e., horizontal distance between two stimulus 740 locations). Additionally, we also included three regressors denoting the similarity of 741 Run (i.e., whether two conditions are within the same run), Subject (i.e., whether two 742 conditions are within the same subject), and Group (i.e., whether two conditions are 743 within the same subject group, according to the stimulus-response mapping). We also 744 added two regressors including ROI-mean fMRI activations for each condition of the 745 pair to remove the possible uni-voxel influence on the RSM. A last term was the 746 intercept. The intercept and slopes of the regressors were set as random effects at the 747 subject level. Individual effects for each regressor were also extracted from the model 748 for statistical inference and brain-behavioral correlation analyses. In brain-behavioral 749 analyses, only the RT was used as behavioral measure to be consistent with the fMRI 750 results, where the error trials were regressed out.

751 The statistical significance of these beta estimates was determined with onesample t-tests (one-tailed). Multiple comparison correction was applied with false 752 discovery rate (FDR) approach⁷³ across all cortical regions ($p_{\text{FDR}} < 0.05$), together 753 754 with a threshold of 0.001 for each region. To test if the representation strengths are 755 different between congruent and incongruent conditions, we also conducted the RDM 756 analyses using only congruent and incongruent trials separately. Individual effects 757 were extracted from each model and tested using a paired t-test. To visualize the 758 difference, we plotted the effect-related patterns (the predictor multiplied by the slope, 759 plus the residual) as a function of the similarity levels (Fig. 4D).

760 Representational connectivity analysis

To explore the possible relevance between the conflict type and the orientation

- regions showing effects, we conducted representational connectivity⁴³ between regions showing
- revidence encoding conflict similarity and orientation similarity. Similar to the RSA
- mentioned above, the z-transformed RSM vector of each region were extracted and

submitted to a mixed linear model, with the RSM of the conflict type region (i.e., the 765 766 right 8C) as the dependent variable, and the RSM of one of the orientation regions 767 (e.g., bilateral V2) as the predictor. Intercept and the slope of the regressor were set as 768 random effects at the subject level, and individual coefficients of the slope were 769 extracted for further statistical analysis. The mixed effect model was conducted for 770 each pair of regions, respectively. Considering there might be strong intrinsic 771 correlations across the RSMs induced by the nuisance factors, such as the within-772 subject similarity, we added two sets of regions as control. First, we selected regions 773 without showing any effects of interest (i.e., $q_{\text{FDR}} > 0.05$ for all the conflict type, 774 orientation, congruency, target, response, spatial Stroop distractor and Simon distractor effects). Second, we selected regions of orientation effect meeting the first 775 776 but not the second criterion, to account for the potential correlation between regions 777 of the two partly orthogonal regressors (Fig. S6). Existence of representational 778 connectivity was defined by a higher connectivity slope than any of the control 779 regions with paired-t tests.

780

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